

SRM VALLIAMMAI ENGINEERING COLLEGE

(An Autonomous Institution)

SRM NAGAR, KATTANKULATHUR-603203

**DEPARTMENT OF INFORMATION TECHNOLOGY
QUESTION BANK**

II SEMESTER



MA3223 -STATISTICAL LEARNING FOR DATA SCIENCE

REGULATION – 2023

ACADEMIC YEAR 2024 – 2025

Prepared by

Mr.L.Mohan, Assistant Professor/ Mathematics



DEPARTMENT OF INFORMATION TECHNOLOGY

SUBJECT: MA3223-STATISTICAL LEARNING FOR DATA SCIENCE

SEM/YEAR: II/I

UNIT – I: PROBABILITY AND RANDOM VARIABLES

12

Random variables (Discrete and continuous)- Moments- Moment generating function-Probability Distributions- Binomial-Poisson- Geometric -Uniform-Exponential-and Normal distribution.

PART – A

Q.No.	Question	BT Level	Competence																
1.	Define probability.	BTL -1	Remembering																
2.	If the random variable X takes the values 1,2,3 and 4 such that $2P(X = 1) = 3P(X = 2) = P(X = 3) = 5P(X = 4)$, find the probability distribution of X	BTL-1	Remembering																
3.	The RV X has the following probability distribution: <table border="1" style="display: inline-table; margin-left: 20px;"> <tr> <td>x</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> </tr> <tr> <td>P(x)</td> <td>0.4</td> <td>k</td> <td>0.2</td> <td>0.3</td> </tr> </table> Find k and the mean value of X	x	-2	-1	0	1	P(x)	0.4	k	0.2	0.3	BTL-2	Understanding						
x	-2	-1	0	1															
P(x)	0.4	k	0.2	0.3															
4.	If three coins are tossed together then what is the Probability that there are exactly 2 heads?	BTL -1	Remembering																
5.	A ball is drawn at random from a box containing 6 red balls, 4 white balls and 5 blue balls. Find the probability that the ball drawn is not red.	BTL2	Understanding																
6.	From a pack of cards, one card is drawn. What is the probability that it is either a spade or a king.	BTL -1	Remembering																
7.	State the theorem of total probability	BTL -1	Remembering																
8.	What is the use of Baye’s theorem?	BTL2	Understanding																
9.	Define continuous random variable with example.	BTL -1	Remembering																
10.	Define discrete random variable with example	BTL -2	Understanding																
11.	Define Moment Generating function of a random variable.	BTL -1	Remembering																
12.	If a random variable X has the MGF $M_X(t) = \frac{2}{2-t}$. Find the mean of X.	BTL -1	Remembering																
13.	Suppose that the life of industrial lamp(in thousands of hours) is exponentially distributed with mean life of 3000 hours, find the probability that the lamp will last between 2000 and 3000 hours.	BTL2	Understanding																
14.	The mean of Binomial distribution is 20 and standard deviation is 4. Find the parameters of the distribution.	BTL2	Understanding																
15.	Find the MGF of Uniform distribution.	BTL2	Understanding																
16.	The number of hardware failures of a computer system in a week of operations has the following p.d.f, Find the mean of the number of failures in a week. <table border="1" style="display: inline-table; margin-left: 20px;"> <tr> <td>No.of failures</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>Probability</td> <td>.18</td> <td>.28</td> <td>.25</td> <td>.18</td> <td>.06</td> <td>.04</td> <td>.01</td> </tr> </table>	No.of failures	0	1	2	3	4	5	6	Probability	.18	.28	.25	.18	.06	.04	.01	BTL2	Understanding
No.of failures	0	1	2	3	4	5	6												
Probability	.18	.28	.25	.18	.06	.04	.01												

17.	The number of hardware failures of a computer system in a week of operations has the following p.d.f, Calculate the value of K.	BTL2	Understanding													
	<table border="1"> <tbody> <tr> <td>No.of failures</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>Probability</td> <td>K</td> <td>2 K</td> <td>2 K</td> <td>K</td> <td>3 K</td> <td>K</td> <td>4 K</td> </tr> </tbody> </table>			No.of failures	0	1	2	3	4	5	6	Probability	K	2 K	2 K	K
No.of failures	0	1	2	3	4	5	6									
Probability	K	2 K	2 K	K	3 K	K	4 K									
18.	If x is a Poisson distribution such that $P(x=1)=4P(x=2)$. Find its mean and variance.	BTL -1	Remembering													
19.	If $f(x) = kx^2, 0 < x < 3$, is to be a density function, find the value of k .	BTL2	Understanding													
20.	A continuous random variable X has p.d.f $f(x) = 2x, 0 \leq x \leq 1$. Find $P(X > 0.5)$.	BTL2	Understanding													
21.	Define Probability.	BTL -1	Remembering													
22.	A normal distribution has mean $\mu = 20$ and standard deviation $\sigma = 10$. Evaluate $(15 \leq X \leq 40)$.	BTL2	Understanding													
23.	Write the axioms of Probability.	BTL -1	Remembering													
24.	Find Mean of Binomial Distribution.															
25.	If X is a normal random variable with mean 3 and variance 9, find the probability that X lies between 2 and 5.	BTL2	Understanding													
PART – B																
1.(a)	Bag I contains 3 red and 4 blue balls while another Bag II contains 5 red and 6 blue balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from second Bag.	BTL -3	Applying													
1.(b)	X speaks truth 4 out of 5 times. A die is thrown. He reports that there is a six. What is the chance that actually there was a six?	BTL -4	Creating													
2.	Out of 2000 families with 4 children each, Find how many family would you expect to have (i) at least 1 boy, (ii) 2 boys, (iii) 1 or 2 girls and iv) no girls	BTL -3	Applying													
3.	The contents of urns I, II, III are as follows: 1 white, 2 black and 3 red balls; 2 white, 1 black and 1 red balls; 4 white, 5 black and 3 red balls; One urn is chosen at random and two balls drawn. They happen to be white and red. What is the probability that they come from urns I, II, III?	BTL -4	Creating													
4.	A factory has 3 machines A1, A2, A3 producing 1000, 2000, 3000 screws per day respectively. A1 produces 1% defectives, A2 produces 1.5% and A3 produces 2% defectives. A screw is chosen at random at the end of a day and found defective. What is the probability that it comes from machines A1?	BTL -3	Applying													
5.(a)	In a bolt factory machines A, B, C manufacture respectively 25, 35 and 40 percent of the total. Of their output 5, 4 and 2 percent are defective bolts respectively. A bolt is drawn at random from the product and is found defective. What are the probabilities that it was manufactured by machines A, B or C?	BTL -4	Creating													
5.(b)	A factory has two machines I and II. Machine I produces 30% of items of the output and Machine II produces 70% of the items. Further 3% of items produced by Machine I are defective and 4% produced by Machine II are defective. If an item is drawn at random, find the probability that it is a defective item.	BTL -3	Applying													

6.(a)	<p>If the discrete random variable X has the probability function given by the table.</p> <table border="1"> <tr> <td>x</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> </tr> <tr> <td>P(x)</td> <td>k/3</td> <td>k/6</td> <td>k/3</td> <td>k/6</td> </tr> </table> <p>Find the value of k and Cumulative distribution of X.</p>	x	1	2	3	4	P(x)	k/3	k/6	k/3	k/6	BTL -4	Creating										
x	1	2	3	4																			
P(x)	k/3	k/6	k/3	k/6																			
6.(b)	Find the MGF of Binomial distribution and hence find its mean and variance	BTL -3	Applying																				
7.(a)	<p>A random variable X has the following probability distribution:</p> <table border="1"> <tr> <td>X</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>P(X)</td> <td>0</td> <td>k</td> <td>2k</td> <td>2k</td> <td>3k</td> <td>k²</td> <td>2k²</td> <td>7k²+k</td> </tr> </table> <p>Find (i) the value of k (ii) $P(1.5 < X < 4.5 / X > 2)$</p>	X	0	1	2	3	4	5	6	7	P(X)	0	k	2k	2k	3k	k ²	2k ²	7k ² +k	BTL -4	Creating		
X	0	1	2	3	4	5	6	7															
P(X)	0	k	2k	2k	3k	k ²	2k ²	7k ² +k															
7.(b)	Find the MGF of Poisson distribution and hence find its mean and variance	BTL -3	Applying																				
8.(a)	Given $\lambda = 4.2$, for a Poisson distribution. Find (a) $P(X \leq 2)$ (b) $P(X \geq 5)$ (c) $P(X = 8)$.	BTL -4	Creating																				
8.(b)	Find the MGF of Exponential distribution and hence find its mean and variance	BTL -3	Applying																				
9.	In an intelligence test administered on 1000 students, the average was 42 and standard deviation 24, find (i) the number of students exceeding a score 50. (ii) the number of students lying between 30 and 54 (iii) the value of score exceeded by top 100 students.	BTL -4	Creating																				
10.	<p>The probability mass function of a discrete R. V X is given in the following table</p> <table border="1"> <tr> <td>X</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <td>P(X)</td> <td>a</td> <td>3a</td> <td>5a</td> <td>7a</td> <td>9a</td> <td>11a</td> <td>13a</td> <td>15a</td> <td>17a</td> </tr> </table> <p>Find (i) the value of a, (ii) $P(X < 3)$, (iii) Mean of X and (iv) Variance of X.</p>	X	0	1	2	3	4	5	6	7	8	P(X)	a	3a	5a	7a	9a	11a	13a	15a	17a	BTL -3	Applying
X	0	1	2	3	4	5	6	7	8														
P(X)	a	3a	5a	7a	9a	11a	13a	15a	17a														
11.	The probability distribution of an infinite discrete distribution is given by $P[X = j] = \frac{1}{2^j}$ ($j = 1, 2, 3, \dots$) Find (i) Mean of X, (ii) $P[X \text{ is even}]$, (iii) $P[X \text{ is odd}]$	BTL -4	Creating																				
12.	<p>A random variable X has a uniform distribution over (-3, 3). Compute</p> <p>(i) $P(X < 2)$ (ii) $P(X < 2)$ (iii) $P(X-2 < 2)$</p> <p>(iv) Find k for which $P(X < k) = 1/3$.</p>	BTL -3	Applying																				
13.	<p>X is a normal variable with mean 30 and standard deviation of 5. Find</p> <p>(i) $P[26 \leq X \leq 40]$ (ii) $P[X \geq 45]$ (iii) $P[X - 30 > 5]$ use normal distribution tables.</p>	BTL -4	Creating																				
14.	Derive the MGF of Uniform distribution and hence find its mean and variance	BTL -3	Applying																				
15.	<p>Buses arrive at a specified stop at 15 minutes interval starting at 7am that is, 7:15, 7:30, 7:45, and so on, If a passenger arrives at the stop at a random time that is uniformly distributed between 7 and 7:30 am, evaluate the probability that he waits</p> <p>(a) Less than 5 minutes for a bus and</p> <p>(b) At least 12 minutes for a bus</p>	BTL -4	Creating																				
16.	State and Prove the memory less property of Exponential distribution	BTL -3	Applying																				

17.	In a test on 2000 electric bulbs, it was found that the life of a particular make, was normally distributed with an average life of 2040 hours and Standard Deviation of 60 hours. Find the number of bulbs likely to burn for (i) more than 2150 hours (ii) less than 1950 hours and (iii) more than 1920 hours burs less than 2160 hours.	BTL -4	Creating
18.(a)	The time (in hours) required to repair a machine is exponentially distributed with parameter $\lambda = 1/2$. (a) What is the probability that the repair time exceeds 2 hours? (b) What is the conditional probability that a repair time exceeds at least 10 hours that its distribution exceeds 9 hours?	BTL -3	Applying
18.(b)	Let X be a Uniformly distributed R. V. over $[-5, 5]$. Evaluate (i) $P(X \leq 2)$ (ii) $P(X > 2)$ (iii) Cumulative distribution function of X (iv) $\text{Var}(X)$	BTL -4	Creating

UNIT II - TWO - DIMENSIONAL RANDOM VARIABLES

12

Joint Probability distribution-Marginal and conditional distribution covariance-correlation and regression line - Central limit theorem.

PART – A

Q.No.	Question	BT Level	Competence			
1.	The equations of two regression lines are $3x+2y=19$ and $3y+9x=46$. Obtain the mean of X and Y.	BTL-1	Remembering			
2.	The joint probability distribution of X and Y is given by $p(x, y) = \frac{x+y}{21}$, $x = 1,2,3; y = 1, 2$. Find the marginal probability distributions of X	BTL-2	Understanding			
3.	Prove that $-1 \leq r_{xy} \leq 1$	BTL-1	Remembering			
4.	State any tow properties of correlation coefficient.	BTL-2	Understanding			
5.	Define Two dimensional Discrete random variables.	BTL-1	Remembering			
6.	The joint probability distribution of X and Y is given by $P(x,y)=7x+4y$ $x = 1, 2; y = 1, 2$. Find the marginal probability distributions of X.	BTL-2	Understanding			
7.	State the correlation coefficient formula.	BTL-1	Remembering			
8.	If $\bar{X} = 970, \bar{Y} = 18, \sigma_x = 38, \sigma_y = 2$ and $r = 0.6$, Find the line of regression of X on Y.	BTL-2	Understanding			
9.	The regression equations are $3x + 2y = 26$ and $6x + y = 31$. Find the correlation coefficient.	BTL-1	Remembering			
10.	What is the acute angle between the two lines of regression?	BTL-2	Understanding			
11.	State Central Limit Theorem.	BTL-1	Remembering			
12.	Define Marginal probability density function of X.	BTL-2	Understanding			
13.	In a partially destroyed laboratory, record of an analysis of correlation data, The following results only are legible; Variance of X = 9; Regression equations are $8X - 10Y + 66 = 0$ and $40X - 18Y = 214$. Find the mean values of X and Y?	BTL-1	Remembering			
14.	Define Two dimensional Continuous random variables.	BTL-2	Understanding			
15.	Find the probability distribution of X + Y from the bi-variate distribution of (X,Y) given below:	BTL-1	Remembering			
	<table border="1" style="display: inline-table; vertical-align: middle;"> <tr> <td style="padding: 5px;">$X \backslash Y$</td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">2</td> </tr> </table>	$X \backslash Y$	1	2		
$X \backslash Y$	1	2				

		1	0.4	0.2													
		2	0.3	0.1													
16.	Let X and Y have the joint p.m.f. Then find $P(X+Y > 1)$	<table border="1"> <tr> <td>Y \ X</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>0</td> <td>0.1</td> <td>0.4</td> <td>0.1</td> </tr> <tr> <td>1</td> <td>0.2</td> <td>0.2</td> <td>0</td> </tr> </table>	Y \ X	0	1	2	0	0.1	0.4	0.1	1	0.2	0.2	0		BTL-2	Understanding
Y \ X	0	1	2														
0	0.1	0.4	0.1														
1	0.2	0.2	0														
17.	Let X and Y be random variables with joint density function $f(x,y) = \begin{cases} 4xy, & 0 < x < 1, 0 < y < 1 \\ 0, & \text{otherwise} \end{cases}$ formulate the value of $E(XY)$				BTL-1	Remembering											
18.	What is the condition for two random variables are independent?				BTL-2	Understanding											
19.	The joint probability density function of random variables (X, Y) is $f(x, y) = k e^{-(2x+3y)}, x \geq 0, y \geq 0$. Find the value of k.				BTL-1	Remembering											
20.	The regression equations are $x + 6y = 14$ and $2x + 3y = 1$. Find the correlation coefficient between X & Y.				BTL-2	Understanding											
21.	The joint probability function (X,Y) is given by $P(x, y) = k(3x + y)$, $x = 0,1$ $y = 1,2$, Find the value of K.				BTL-1	Remembering											
22.	If the joint pdf of (X, Y) is $f(x, y) = \begin{cases} \frac{1}{4}, & 0 < x, y < 2 \\ 0, & \text{otherwise} \end{cases}$. Find $P(X + Y \leq 1)$				BTL-2	Understanding											
23.	If the joint probability density function of a random variable X and Y is given by $f(x, y) = \begin{cases} \frac{x^3 y^3}{16}, & 0 < x < 2, 0 < y < 2 \\ 0, & \text{otherwise} \end{cases}$. Find the marginal density function of X.				BTL-1	Remembering											
24.	The joint probability density of a two dimensional random variable (X, Y) is given by $f(x, y) = \begin{cases} kxe^{-y}; & 0 \leq x < 2, y > 0 \\ 0, & \text{otherwise} \end{cases}$. Evaluate k.				BTL-2	Understanding											
25.	The equations of two regression lines are $3x+2y=19$ and $3y+9x=46$. Derive the correlation coefficient between X and Y.				BTL-1	Remembering											
PART – B																	
1.	The two dimensional random variable (X, Y) has the joint probability mass function $f(x, y) = \frac{x+2y}{27}, x = 0,1,2; y = 0,1,2$. Find the conditional distribution of Y given X = 1 also find the conditional distribution of X given Y = 1.				BTL -3	Applying											

2.	<p>From the following table for bivariate distribution of (X, Y). Find (i) $P(X \leq 1)$ (ii) $P(Y \leq 3)$ (iii) $P(X \leq 1, Y \leq 3)$ (iv) $P(X \leq 1 / Y \leq 3)$ (v) $P(Y \leq 3 / X \leq 1)$</p> <table border="1" data-bbox="229 259 1155 647"> <thead> <tr> <th>Y \ X</th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> <th>6</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> <td>$\frac{1}{32}$</td> <td>$\frac{2}{32}$</td> <td>$\frac{2}{32}$</td> <td>$\frac{3}{32}$</td> </tr> <tr> <td>1</td> <td>$\frac{1}{16}$</td> <td>$\frac{1}{16}$</td> <td>$\frac{1}{8}$</td> <td>$\frac{1}{8}$</td> <td>$\frac{1}{8}$</td> <td>$\frac{1}{8}$</td> </tr> <tr> <td>2</td> <td>$\frac{1}{32}$</td> <td>$\frac{1}{32}$</td> <td>$\frac{1}{64}$</td> <td>$\frac{1}{64}$</td> <td>0</td> <td>$\frac{2}{64}$</td> </tr> </tbody> </table>	Y \ X	1	2	3	4	5	6	0	0	0	$\frac{1}{32}$	$\frac{2}{32}$	$\frac{2}{32}$	$\frac{3}{32}$	1	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$	2	$\frac{1}{32}$	$\frac{1}{32}$	$\frac{1}{64}$	$\frac{1}{64}$	0	$\frac{2}{64}$	BTL -4	Creating
Y \ X	1	2	3	4	5	6																									
0	0	0	$\frac{1}{32}$	$\frac{2}{32}$	$\frac{2}{32}$	$\frac{3}{32}$																									
1	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$																									
2	$\frac{1}{32}$	$\frac{1}{32}$	$\frac{1}{64}$	$\frac{1}{64}$	0	$\frac{2}{64}$																									
3	<p>If X, Y are RV's having the joint density function $f(x, y) = k(6 - x - y), 0 < x < 2, 2 < y < 4$, Find (i) $P(x < 1, y < 3)$ (ii) $P(x < 1 / y < 3)$ (iii) $P(y < 3 / x < 1)$</p>	BTL -3	Applying																												
4(a).	<p>The joint distribution of X and Y is given by $f(x, y) = \frac{x+y}{21}$, $x = 1, 2, 3; y = 1, 2$. Find the marginal distributions of X and Y.</p>	BTL -4	Creating																												
4(b).	<p>The joint pdf a bivariate R.V(X, Y) is given by $f(x, y) =$ $\begin{cases} Kxy & ; 0 < x < 1, 0 < y < 1 \\ 0 & , \text{ otherwise} \end{cases}$ Find (1) K, (2) Are X and Y independent R.V's.</p>	BTL -3	Applying																												
5.	<p>If the joint pdf of (X, Y) is given by $P(x, y) = K(2x+3y)$, $x=0, 1, 2$, $y = 1, 2, 3$ Find all the marginal probability distribution. Also find the probability distribution of X+Y.</p>	BTL -4	Creating																												
6(a).	<p>Three balls are drawn at random without replacement from a box containing 2 white, 3 red and 4 blue balls. If X denotes the number of white balls drawn and Y denotes the number of red balls drawn, Identify the probability distribution of X and Y.</p>	BTL -3	Applying																												
6(b).	<p>The joint pdf of (X, Y) is $f(x, y) = e^{-(x+y)}, 0 \leq x < \infty, 0 \leq y < \infty$. Are X and Y independent?</p>	BTL -4	Creating																												
7.	<p>If the joint pdf of a two-dimensional RV(X, Y) is given by $f(x, y) = \begin{cases} x^2 + \frac{xy}{3}; & 0 < x < 1, 0 < y < 2 \\ 0, & \text{ elsewhere} \end{cases}$. Find (i) $P(X > \frac{1}{2})$ (iii) $P(Y < \frac{1}{2} / X < \frac{1}{2})$</p>	BTL -3	Applying																												
8	<p>The joint pdf of a two dimensional random variable (X, Y) is given by $f(x, y) = xy^2 + \frac{x^2}{8}, 0 \leq x \leq 2, 0 \leq y \leq 1$. Compute (i) $P(Y < 1/2)$ (ii) $P(X > 1 / Y < \frac{1}{2})$ (iii) $P(Y < \frac{1}{2} / X > 1)$</p>	BTL -4	Creating																												
9.	<p>From the following data, Find (i) The two regression equations (ii) The coefficient of correlation between the marks in Mathematics and Statistics (iii) The most likely marks in Statistics when marks in Mathematics are 30 Marks in Maths: 25 28 35 32 31 36 29 38 34 32 Marks in Statistics: 43 46 49 41 36 32 31 30 33 39</p>	BTL -3	Applying																												
10(a).	<p>If $f(x, y) = \frac{6-x-y}{8}, 0 \leq x \leq 2, 2 \leq y \leq 4$ for a bivariate random variable (X, Y), Find the correlation coefficient ρ.</p>	BTL -4	Creating																												

10(b).	If $X_1, X_2, X_3, \dots, X_n$ are Poisson variates with mean 2, use central limit theorem to estimate $P(120 < S_n < 160)$ where $S_n = X_1 + X_2 + X_3 + \dots + X_n$ and $n=75$.	BTL -3	Applying																				
11.	Find the correlation coefficient for the following heights of fathers X, their sons Y and also find the equations of regression lines. Hence find the height of son when the height of father is 71 <table border="1" style="margin-left: 20px;"> <tbody> <tr> <td>X</td> <td>65</td> <td>66</td> <td>67</td> <td>67</td> <td>68</td> <td>69</td> <td>70</td> <td>72</td> </tr> <tr> <td>Y</td> <td>67</td> <td>68</td> <td>65</td> <td>68</td> <td>72</td> <td>72</td> <td>69</td> <td>71</td> </tr> </tbody> </table>	X	65	66	67	67	68	69	70	72	Y	67	68	65	68	72	72	69	71	BTL -4	Creating		
X	65	66	67	67	68	69	70	72															
Y	67	68	65	68	72	72	69	71															
12.	State and Prove Chebyshev's inequality	BTL -3	Applying																				
13(a).	The equation of two regression lines obtained by in a correlation analysis is as follows: $5x - y = 22$, $64x - 45y = 24$. (i) Calculate the correlation coefficient (ii) Mean value of X & Y.	BTL -4	Creating																				
13(b).	The lifetime of a certain brand of an electric bulb may be considered a RV with mean 1200h and standard deviation 250h. Find the probability, using central limit theorem, that the average life time of 60 bulbs exceeds 1250 h.	BTL -3	Applying																				
14.	Two random variables X and Y have the joint density $f(x,y) = \begin{cases} 2 - x - y, & 0 < x < 1, 0 < y < 1 \\ 0, & \text{otherwise} \end{cases}$ Show that the Correlation coefficient between X and Y is $-1/11$.	BTL -4	Creating																				
15.	The following table represents the joint probability distribution of the discrete RV (X,Y). Find all the marginal and conditional distributions. <table border="1" style="margin-left: 20px;"> <thead> <tr> <th rowspan="2">Y</th> <th colspan="3">X</th> </tr> <tr> <th>1</th> <th>2</th> <th>3</th> </tr> </thead> <tbody> <tr> <th>1</th> <td>1/2</td> <td>1/6</td> <td>0</td> </tr> <tr> <th>2</th> <td>0</td> <td>1/9</td> <td>1/5</td> </tr> <tr> <th>3</th> <td>1/18</td> <td>1/4</td> <td>2/15</td> </tr> </tbody> </table>	Y	X			1	2	3	1	1/2	1/6	0	2	0	1/9	1/5	3	1/18	1/4	2/15	BTL -3	Applying	
Y	X																						
	1	2	3																				
1	1/2	1/6	0																				
2	0	1/9	1/5																				
3	1/18	1/4	2/15																				
16.	The equation of two regression lines obtained by in a correlation analysis is as follows: $3x + 12y = 19$, $3y + 9x = 46$. (i) Calculate the correlation coefficient (ii) Mean value of X & Y.	BTL -4	Creating																				
17.	Find the Coefficient of Correlation between industrial production and export using the following table <table border="1" style="margin-left: 20px;"> <tbody> <tr> <td>Production (X)</td> <td>14</td> <td>17</td> <td>23</td> <td>21</td> <td>25</td> </tr> <tr> <td>Export (Y)</td> <td>10</td> <td>12</td> <td>15</td> <td>20</td> <td>23</td> </tr> </tbody> </table>	Production (X)	14	17	23	21	25	Export (Y)	10	12	15	20	23	BTL -3	Applying								
Production (X)	14	17	23	21	25																		
Export (Y)	10	12	15	20	23																		
18.	Obtain the lines of regression <table border="1" style="margin-left: 20px;"> <tbody> <tr> <td>X</td> <td>50</td> <td>55</td> <td>50</td> <td>60</td> <td>65</td> <td>65</td> <td>65</td> <td>60</td> <td>60</td> </tr> <tr> <td>Y</td> <td>11</td> <td>14</td> <td>13</td> <td>16</td> <td>16</td> <td>15</td> <td>15</td> <td>14</td> <td>13</td> </tr> </tbody> </table>	X	50	55	50	60	65	65	65	60	60	Y	11	14	13	16	16	15	15	14	13	BTL -4	Creating
X	50	55	50	60	65	65	65	60	60														
Y	11	14	13	16	16	15	15	14	13														

UNIT - III: TESTING OF HYPOTHESIS

12

Sampling distributions - Tests for single mean and difference of means (Large and small samples)
 – Tests for single variance and equality of variances.

PART – A

Q.No.	Question	BT Level	Competence
1.	Define Statistics	BTL -1	Remembering
2.	Define Parameter.	BTL -1	Remembering
3.	In a large city A, 20 percent of a random sample of 900 school boys had a slight physical defect. In another large city B, 18.5 percent of a random sample of 1600 school boys had some defect. Is the difference between the proportions significant?	BTL -2	Understanding

4.	Write down the formula of test statistic 't' to test the significance of difference between the means.	BTL -1	Applying																								
5.	State any two applications of t-test.	BTL -2	Creating																								
6.	Explain null and alternate hypothesis.	BTL -1	Remembering																								
7.	Mention the various steps involved in testing of hypothesis.	BTL -1	Remembering																								
8.	Define 'F' variate.	BTL -1	Analyzing																								
9.	What is the assumption of t-test?	BTL -2	Analyzing																								
10.	Give the main use of small sample test	BTL -1	Creating																								
11.	What are the expected frequencies of 2x2 contingency table? <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>A</td> <td>b</td> </tr> <tr> <td>C</td> <td>d</td> </tr> </tbody> </table>	A	b	C	d	BTL -2	Analyzing																				
A	b																										
C	d																										
12.	Write the formula for the chi- square test of goodness of fit of a random sample to a hypothetical distribution.	BTL -1	Analyzing																								
13.	What are the properties of "F" test?	BTL -2	Applying																								
14.	Write the application of 'F' test.	BTL -1	Analyzing																								
15.	Define Type I and Type II error.	BTL -2	Understanding																								
16.	What is the essential difference between confidence limits and tolerance limits?	BTL -1	Remembering																								
17.	State level of significance.	BTL -1	Remembering																								
18.	Twenty people were attacked by a disease and only 18 were survived. The hypothesis is set in such a way that the survival rate is 85% if attacked by this disease. Will you reject the hypothesis that it is more at 5% level. ($Z_{0.05} = 1.645$).	BTL -2	Understanding																								
19.	A standard sample of 200 tins of coconut oil gave an average weight of 4.95 kg with a standard deviation of 0.21 kg. Do we accept that the net weight is 5 kg per tin at 5% level of significance?	BTL -2	Understanding																								
20.	What are the applications of t-test?	BTL -2	Applying																								
21.	What are the parameters and statistics in sampling	BTL -1	Remembering																								
22.	A random sample of 25 cups from a certain coffee dispensing machine yields a mean $\bar{x} = 6.9$ occurs per cup. Use 0.05 level of significance to test, on the average, the machine dispense $\mu = 7.0$ ounces against the null hypothesis that, on the average, the machine dispenses $\mu < 7.0$ ounces. Assume that the distribution of ounces per cup is normal, and that the variance is the known quantity $\sigma^2 = 0.01$ ounces	BTL -2	Understanding																								
23.	Define Standard Error.	BTL -1	Remembering																								
24.	A standard sample of 100 tins of coconut oil gave an average weight of 3.92 kg with a standard deviation of 0.11 kg. Do we accept that the net weight is 5 kg per tin at 1% level of significance?	BTL -1	Analyzing																								
25.	Write the formula for Z-test in Single mean and Difference mean	BTL -1	Remembering																								
PART – B																											
1.(a)	A group of 10 rats fed on diet A and another group of 8 rats fed on diet B, Recorded the following increase the following increase in weight.(gm) <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>Diet A</td> <td>5</td> <td>6</td> <td>8</td> <td>1</td> <td>12</td> <td>4</td> <td>3</td> <td>9</td> <td>6</td> <td>10</td> </tr> <tr> <td>Diet B</td> <td>2</td> <td>3</td> <td>6</td> <td>8</td> <td>10</td> <td>1</td> <td>2</td> <td>8</td> <td>-</td> <td>-</td> </tr> </tbody> </table> <p>Find the variances are significantly different. (Use F-test)</p>	Diet A	5	6	8	1	12	4	3	9	6	10	Diet B	2	3	6	8	10	1	2	8	-	-	BTL -3	Applying		
Diet A	5	6	8	1	12	4	3	9	6	10																	
Diet B	2	3	6	8	10	1	2	8	-	-																	
1.(b)	The marks obtained by a group of 9 regular course students and another group of 11 part time course students in a test are given below <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>Sample I</td> <td>56</td> <td>62</td> <td>63</td> <td>54</td> <td>60</td> <td>51</td> <td>67</td> <td>69</td> <td>58</td> <td></td> <td></td> </tr> <tr> <td>Sample II</td> <td>62</td> <td>70</td> <td>71</td> <td>62</td> <td>60</td> <td>56</td> <td>75</td> <td>64</td> <td>72</td> <td>68</td> <td>66</td> </tr> </tbody> </table>	Sample I	56	62	63	54	60	51	67	69	58			Sample II	62	70	71	62	60	56	75	64	72	68	66	BTL -4	Creating
Sample I	56	62	63	54	60	51	67	69	58																		
Sample II	62	70	71	62	60	56	75	64	72	68	66																

	Examine whether the marks obtained by regular students and part-time students differ significantly at 5% levels of significance.																		
2.	Records taken of the number of male and female births in 800 families having four Children are as follows : Number of male births : 0 1 2 3 4 Number of female births : 4 3 2 1 0 Number of Families : 32 178 290 236 64 Infer whether the data are consistent with the hypothesis that the binomial law holds the chance of a male birth is equal to female birth, namely $p = \frac{1}{2} = q$.	BTL -3	Applying																
3.	The nicotine content in milligram of two samples of tobacco where found to be as follows Sample 1 24 27 26 21 25 Sample 2 27 30 28 31 22 36 Can it be said that this samples where from normal population with the same mean.	BTL -4	Creating																
4.	Mechanical engineers testing a new arc welding technique, classified welds both with respect to appearance and an X-ray inspection <table border="1"> <thead> <tr> <th>X-ray/Appearance</th> <th>Bad</th> <th>Normal</th> <th>Good</th> </tr> </thead> <tbody> <tr> <td>Bad</td> <td>20</td> <td>7</td> <td>3</td> </tr> <tr> <td>Normal</td> <td>13</td> <td>51</td> <td>16</td> </tr> <tr> <td>Good</td> <td>7</td> <td>12</td> <td>21</td> </tr> </tbody> </table> Test for independence using 0.05 level of significance.	X-ray/Appearance	Bad	Normal	Good	Bad	20	7	3	Normal	13	51	16	Good	7	12	21	BTL -3	Applying
X-ray/Appearance	Bad	Normal	Good																
Bad	20	7	3																
Normal	13	51	16																
Good	7	12	21																
5.	Two random samples gave the following results: <table border="1"> <thead> <tr> <th>Sample</th> <th>Size</th> <th>Sample mean</th> <th>Sum of squares of deviation from the mean</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>10</td> <td>15</td> <td>90</td> </tr> <tr> <td>2</td> <td>12</td> <td>14</td> <td>108</td> </tr> </tbody> </table> Analyze whether the samples have come from the same normal population.	Sample	Size	Sample mean	Sum of squares of deviation from the mean	1	10	15	90	2	12	14	108	BTL -4	Creating				
Sample	Size	Sample mean	Sum of squares of deviation from the mean																
1	10	15	90																
2	12	14	108																
6.	Random samples drawn from two places gave the following data relating to the heights of male adults: <table border="1"> <thead> <tr> <th></th> <th>Place A</th> <th>Place B</th> </tr> </thead> <tbody> <tr> <td>Mean height (in inches)</td> <td>68.50</td> <td>65.50</td> </tr> <tr> <td>S.D (in inches)</td> <td>2.5</td> <td>3.0</td> </tr> <tr> <td>No. of adult males in sample</td> <td>1200</td> <td>1500</td> </tr> </tbody> </table> Test at 5 % level, that the mean height is the same for adults in the two places.		Place A	Place B	Mean height (in inches)	68.50	65.50	S.D (in inches)	2.5	3.0	No. of adult males in sample	1200	1500	BTL -3	Applying				
	Place A	Place B																	
Mean height (in inches)	68.50	65.50																	
S.D (in inches)	2.5	3.0																	
No. of adult males in sample	1200	1500																	
7.	The following data gives the number of aircraft accidents that occurred during the various days of a week. Find whether the accidents are uniformly distributed over the week <table border="1"> <thead> <tr> <th>Days</th> <th>Sun</th> <th>Mon</th> <th>Tues</th> <th>Wed</th> <th>Thu</th> <th>Fri</th> <th>Sat</th> </tr> </thead> <tbody> <tr> <td>No. of accidents</td> <td>14</td> <td>16</td> <td>08</td> <td>12</td> <td>11</td> <td>9</td> <td>14</td> </tr> </tbody> </table>	Days	Sun	Mon	Tues	Wed	Thu	Fri	Sat	No. of accidents	14	16	08	12	11	9	14	BTL -4	Creating
Days	Sun	Mon	Tues	Wed	Thu	Fri	Sat												
No. of accidents	14	16	08	12	11	9	14												
8.	The nicotine content in milligram of two samples of tobacco where found to be as follows, test the significant difference between means of the two samples. <table border="1"> <tbody> <tr> <td>Sample I</td> <td>21</td> <td>24</td> <td>25</td> <td>26</td> <td>27</td> <td>-</td> </tr> <tr> <td>Sample II</td> <td>22</td> <td>27</td> <td>28</td> <td>30</td> <td>31</td> <td>36</td> </tr> </tbody> </table>	Sample I	21	24	25	26	27	-	Sample II	22	27	28	30	31	36	BTL -3	Applying		
Sample I	21	24	25	26	27	-													
Sample II	22	27	28	30	31	36													
9.	Test of fidelity and selectivity of 190 radio receivers produced the results shown in the following table	BTL -4	Creating																

		Fidelity								
		Selectivity	Low	Average	High					
		Low	6	12	32					
		Average	33	61	18					
		High	13	15	0					
		Use 0.01 level of significance to test whether there is a relationship between fidelity and selectivity.								
10.	Two independent samples of sizes 8 and 7 contained the following values.								BTL -3	Applying
		Sample I	19	17	15	21	16	18	16	14
		Sample II	15	14	15	19	15	18	16	
		Test if the two populations have the same mean.								
11.	Samples of two types of electric bulbs were tested for length of life and following data were obtained.								BTL -4	Creating
		Type I			Type II					
		Sample Size	8			7				
		Sample Mean	1234hrs			1036hrs				
		Sample S.D	36hrs			40hrs				
		Analyze that, is the difference in the means sufficient to warrant that type I is superior to type II regarding the length of life?								
12.	Two independent samples of 8 and 7 items respectively had the following Values of the variable (weight in kgs.) Use 0.05 LOS to								BTL -3	Applying
		Sample I	9	11	13	11	15	9	12	14
		Sample II	10	12	10	14	9	8	10	
		test whether the variances of the two population's sample are equal.								
13.	A survey of 320 families with 5 children each revealed the following distribution								BTL -4	Creating
		Boys	5	4	3	2	1	0		
		Girls	0	1	2	3	4	5		
		Families	14	56	110	88	40	12		
		Is this result consistent with the hypothesis that male and female births are equally probable?								
14.	In a certain factory there are two independent processes manufacturing the same item. The average weight in a sample of 250 items produced from one process is found to be 120 Ozs, with a standard deviation of 12 Ozs, while the corresponding figures in a sample of 400 items from the other process are 124 and 14. Is the difference between the two sample means significant?								BTL -3	Applying
15. (a)	A simple sample of heights of 6400 Englishmen has a mean of 170cms and a standard deviation of 6.4cms, while a simple sample of heights of 1600 Americans has a mean of 172 cm and a standard deviation of 6.3cms. Do the data indicate that Americans are, on the average, taller than Englishmen?								BTL -4	Creating
15.(b)	A sample of 100 students is taken from a large population. The mean height of the students in this sample is 160cms. Can it be reasonably regarded that this sample is from a population of mean 165 cm and standard deviation 10 cm?								BTL -3	Applying
16.	The heights of 10 males of a given locality are found to be 70, 67, 62, 68, 61, 68, 70, 64, 64, 66 inches. Is it reasonable to believe that the average height is grater than 64 inches?								BTL -4	Creating

17.	In a sample of 8 observations, the sum of squares of deviation of the sample values from the sample mean was 84.4 and in the other sample of 10 observations it was 102.6. Test whether this difference is significant at 5% level, given that the 5% point of F for $v_1=7$ and $v_2=9$ degrees of freedom is 3.27	BTL -3	Applying
18.	The mean breaking strength of the cables supplied by manufacture is 1800 with S.D 100. By a new technique in the manufacturing process it is claimed that the breaking strength of the cable has increased. To test this claim a sample of 50 cables is tested and is found that the mean breaking strength is 1850. Can we support the claim at 1% level of significance.	BTL -4	Creating

UNIT-IV: PARAMETRIC TESTS

12

Chi-square tests for independence of attributes and goodness of fit – Design of experiments one way and two way classification.

PART – A

Q.No	Question	BT Level	Competence
1.	What is ANOVA?	BTL -1	Remembering
2.	What are the uses of ANOVA?	BTL -1	Remembering
3.	What are the components of design of experiment?	BTL -1	Remembering
4.	Write the basic assumptions in analysis of variance.	BTL -1	Remembering
5.	What are the basic principles of Experimental Design?	BTL-1	Applying
6.	Define experimental error.	BTL-2	Understanding
7.	Write any two advantages of RBD over CRD.	BTL -1	Remembering
8.	What is the aim of design of experiments?	BTL -2	Understanding
9.	What is the degrees of freedom for Error in one way classification?	BTL -2	Understanding
10.	What is the degrees of freedom for Error in Two way classification?	BTL -2	Understanding
11.	What is the degrees of freedom for Sum of Squares due to Treatments in One-way Classification?	BTL -1	Applying
12.	What is the TSS degrees of freedom for Two-way Classification with r – rows and c – columns?	BTL-1	Remembering
13.	What is meant by tolerance limits?	BTL -2	Applying
14.	What are the basic elements of a Completely Randomized Experimental Design?	BTL -1	Analyzing
15.	When do you apply analysis of variance technique?	BTL -1	Analyzing
16.	Define Replication	BTL -2	Analyzing
17.	What is a completely randomized design.	BTL -2	Analyzing
18.	Explain the advantages of a Latin square design?	BTL -2	Analyzing
19.	Demonstrate the purpose of blocking in a randomized block design?	BTL -1	Creating
20.	State the Basic principles of the design of experiment?	BTL -2	Creating
21.	Why a 2×2 Latin square is not possible? Explain.	BTL-1	Remembering
22.	Demonstrate main advantage of Latin square Design over Randomized Block Design?	BTL-1	Remembering
23.	Analyze the advantages of the Latin square design over the other design.	BTL-2	Understanding
24.	Write any two differences between RBD and LSD.	BTL-2	Understanding
25.	Define Randomization		

Part B

1.	<p>The accompanying data resulted from an experiment comparing the degree of soiling for fabric copolymerized with the 3 different mixtures of met acrylic acid. Analyze the classification.</p> <p>Mixture 1 : 0.56 1.12 0.90 1.07 0.94 Mixture 2 : 0.72 0.69 0.87 0.78 0.91 Mixture 3 : 0.62 1.08 1.07 0.99 0.93</p>	BTL -3	Applying																															
2.	<p>The following table shows the lives in hours of four brands of electric lamps brand</p> <p>A: 1610, 1610, 1650, 1680, 1700, 1720, 1800 B: 1580, 1640, 1640, 1700, 1750 C: 1460, 1550, 1600, 1620, 1640, 1660, 1740, 1820 D: 1510, 1520, 1530, 1570, 1600, 1680</p> <p>Identify an analysis of variance and test the homogeneity of the mean lives of the four brands of lamps.</p>	BTL -4	Creating																															
3.	<p>A sample of 200 persons with a particular disease was selected. Out of these, 100 were given a drug and the others were not given any drug. The result are as follows:</p> <table border="1"> <thead> <tr> <th>Number of persons</th> <th>Drug</th> <th>No drug</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Cured</td> <td>65</td> <td>55</td> <td>120</td> </tr> <tr> <td>Not cured</td> <td>35</td> <td>45</td> <td>80</td> </tr> <tr> <td>Total</td> <td>100</td> <td>100</td> <td>200</td> </tr> </tbody> </table> <p>Test whether the drug is effective or not?</p>	Number of persons	Drug	No drug	Total	Cured	65	55	120	Not cured	35	45	80	Total	100	100	200	BTL -3	Applying															
Number of persons	Drug	No drug	Total																															
Cured	65	55	120																															
Not cured	35	45	80																															
Total	100	100	200																															
4.	<p>A random sample is selected from each of 3 makes of ropes and their braking strength are measured with the following results.</p> <p>I : 70 72 75 80 83 II : 100 110 108 112 113 120 107 III : 60 65 57 84 87 73</p> <p>Test whether the braking strehgh of the ropes differs significantly?</p>	BTL -4	Creating																															
5.	<p>Given the following table for hair color and eye color, identify the value of Chi-square. Is there good association between hair color and eye color?</p> <table border="1"> <thead> <tr> <th colspan="2" rowspan="2"></th> <th colspan="4">Hair color</th> </tr> <tr> <th>Fair</th> <th>Brown</th> <th>Black</th> <th>Total</th> </tr> </thead> <tbody> <tr> <th rowspan="4">Eye color</th> <th>Blue</th> <td>15</td> <td>5</td> <td>20</td> <td>40</td> </tr> <tr> <th>Grey</th> <td>20</td> <td>10</td> <td>20</td> <td>50</td> </tr> <tr> <th>Brown</th> <td>25</td> <td>15</td> <td>20</td> <td>60</td> </tr> <tr> <th>Total</th> <td>60</td> <td>30</td> <td>60</td> <td>150</td> </tr> </tbody> </table>			Hair color				Fair	Brown	Black	Total	Eye color	Blue	15	5	20	40	Grey	20	10	20	50	Brown	25	15	20	60	Total	60	30	60	150	BTL -3	Applying
				Hair color																														
		Fair	Brown	Black	Total																													
Eye color	Blue	15	5	20	40																													
	Grey	20	10	20	50																													
	Brown	25	15	20	60																													
	Total	60	30	60	150																													
6.	<p>A random sample is selected from each of three makes of ropes and their breaking strength (in pounds) are measured with the following results</p> <p>Sample I : 70 72 75 80 83 Sample II : 100 110 108 112 113 120 107 Sample III: 60 65 57 84 87 73</p> <p>Test whether the breaking strength of the ropes differs significantly?</p>	BTL -4	Creating																															
7.	<p>Ten persons were appointed in the officer cadre in an office. Their performance was noted by giving a test and marks were recorded out of 100.</p> <p>Employee : A B C D E F G H I J Before Training : 80 76 92 60 70 56 74 56 70 56 After Training : 84 70 96 80 70 52 84 72 72 50</p> <p>By applying t-test can it be concluded that the employees have been benefited by the training?</p>	BTL -3	Applying																															
8.	<p>Five doctors each test five treatments for a certain disease and observe the number of days each patient takes to recover. The results are as follows</p>	BTL -4	Creating																															

	(recovery time in days)																																												
	<table border="1"> <thead> <tr> <th></th> <th colspan="5">Treatment</th> </tr> <tr> <th>Doctor</th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>10</td> <td>14</td> <td>23</td> <td>18</td> <td>20</td> </tr> <tr> <td>B</td> <td>11</td> <td>15</td> <td>24</td> <td>17</td> <td>21</td> </tr> <tr> <td>C</td> <td>9</td> <td>12</td> <td>20</td> <td>16</td> <td>19</td> </tr> <tr> <td>D</td> <td>8</td> <td>13</td> <td>17</td> <td>17</td> <td>20</td> </tr> <tr> <td>E</td> <td>12</td> <td>15</td> <td>19</td> <td>15</td> <td>22</td> </tr> </tbody> </table>		Treatment					Doctor	1	2	3	4	5	A	10	14	23	18	20	B	11	15	24	17	21	C	9	12	20	16	19	D	8	13	17	17	20	E	12	15	19	15	22		
	Treatment																																												
Doctor	1	2	3	4	5																																								
A	10	14	23	18	20																																								
B	11	15	24	17	21																																								
C	9	12	20	16	19																																								
D	8	13	17	17	20																																								
E	12	15	19	15	22																																								
	Estimate the difference between (a) doctors and (b) treatments for the above data at 5% level.																																												
9.	Perform a 2-way ANOVA on the data given below:																																												
	<table border="1"> <thead> <tr> <th colspan="2"></th> <th colspan="3">Treatment 1</th> </tr> <tr> <th colspan="2"></th> <th>1</th> <th>2</th> <th>3</th> </tr> </thead> <tbody> <tr> <th rowspan="5">Treatment 2</th> <th>1</th> <td>30</td> <td>26</td> <td>38</td> </tr> <tr> <th>2</th> <td>24</td> <td>29</td> <td>28</td> </tr> <tr> <th>3</th> <td>33</td> <td>24</td> <td>35</td> </tr> <tr> <th>4</th> <td>36</td> <td>31</td> <td>30</td> </tr> <tr> <th>5</th> <td>27</td> <td>35</td> <td>33</td> </tr> </tbody> </table>			Treatment 1					1	2	3	Treatment 2	1	30	26	38	2	24	29	28	3	33	24	35	4	36	31	30	5	27	35	33	BTL -3	Applying											
		Treatment 1																																											
		1	2	3																																									
Treatment 2	1	30	26	38																																									
	2	24	29	28																																									
	3	33	24	35																																									
	4	36	31	30																																									
	5	27	35	33																																									
	Use the coding method subtracting 30 from the given no.																																												
10.	A chemist wishes to test the effect of four chemical agents on the strength of a particular type of cloth. Because there might be variability from one bolt to another, the chemist decides to use a randomized block design, with the bolts of cloth considered as blocks, she selects five bolts and applies all four chemicals in random order to each bolt. The resulting tensile strength follows																																												
	<table border="1"> <thead> <tr> <th colspan="2"></th> <th colspan="5">BOLT</th> </tr> <tr> <th colspan="2"></th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> </tr> </thead> <tbody> <tr> <th rowspan="4">CHEMICAL</th> <th>1</th> <td>73</td> <td>68</td> <td>74</td> <td>71</td> <td>67</td> </tr> <tr> <th>2</th> <td>73</td> <td>67</td> <td>75</td> <td>72</td> <td>70</td> </tr> <tr> <th>3</th> <td>75</td> <td>68</td> <td>78</td> <td>73</td> <td>68</td> </tr> <tr> <th>4</th> <td>73</td> <td>71</td> <td>75</td> <td>75</td> <td>69</td> </tr> </tbody> </table>			BOLT							1	2	3	4	5	CHEMICAL	1	73	68	74	71	67	2	73	67	75	72	70	3	75	68	78	73	68	4	73	71	75	75	69	BTL -4	Creating			
		BOLT																																											
		1	2	3	4	5																																							
CHEMICAL	1	73	68	74	71	67																																							
	2	73	67	75	72	70																																							
	3	75	68	78	73	68																																							
	4	73	71	75	75	69																																							
	Does the tensile strength depend on chemical? Test at 10% level of significance.																																												
11.	The following data gives the number of aircraft accidents that occurred during the various days of a week. Find whether the accidents are uniformly distributed over the week																																												
	<table border="1"> <thead> <tr> <th>Days</th> <th>Sun</th> <th>Mon</th> <th>Tues</th> <th>Wed</th> <th>Thu</th> <th>Fri</th> <th>Sat</th> </tr> </thead> <tbody> <tr> <td>No. of accidents</td> <td>14</td> <td>16</td> <td>08</td> <td>12</td> <td>11</td> <td>9</td> <td>14</td> </tr> </tbody> </table>	Days	Sun	Mon	Tues	Wed	Thu	Fri	Sat	No. of accidents	14	16	08	12	11	9	14	BTL -3	Applying																										
Days	Sun	Mon	Tues	Wed	Thu	Fri	Sat																																						
No. of accidents	14	16	08	12	11	9	14																																						
12.	Four different though supposedly equivalent forms of a standardized reading achievement test were given to each of 5 students and the following are the scores, which they obtained																																												
	<table border="1"> <thead> <tr> <th colspan="2"></th> <th colspan="5">Student</th> </tr> <tr> <th colspan="2"></th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> </tr> </thead> <tbody> <tr> <th rowspan="4">Form</th> <th>A</th> <td>75</td> <td>73</td> <td>59</td> <td>69</td> <td>84</td> </tr> <tr> <th>B</th> <td>83</td> <td>72</td> <td>56</td> <td>70</td> <td>92</td> </tr> <tr> <th>C</th> <td>86</td> <td>61</td> <td>53</td> <td>72</td> <td>88</td> </tr> <tr> <th>D</th> <td>73</td> <td>67</td> <td>62</td> <td>79</td> <td>95</td> </tr> </tbody> </table>			Student							1	2	3	4	5	Form	A	75	73	59	69	84	B	83	72	56	70	92	C	86	61	53	72	88	D	73	67	62	79	95	BTL -4	Creating			
		Student																																											
		1	2	3	4	5																																							
Form	A	75	73	59	69	84																																							
	B	83	72	56	70	92																																							
	C	86	61	53	72	88																																							
	D	73	67	62	79	95																																							
	Perform a two way analysis of variance to test at the level of significance 1%.																																												

13.	<p>A company appoints 4 salesmen A, B, C and D and observes their sales in 3 seasons, summer winter and monsoon. The figures are given in the following table:</p> <table border="1" data-bbox="379 241 1023 434"> <thead> <tr> <th></th> <th colspan="4">Salesmen</th> </tr> <tr> <th>Season</th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> </tr> </thead> <tbody> <tr> <td>Summer</td> <td>45</td> <td>40</td> <td>28</td> <td>37</td> </tr> <tr> <td>Winter</td> <td>43</td> <td>41</td> <td>45</td> <td>38</td> </tr> <tr> <td>Monsoon</td> <td>39</td> <td>39</td> <td>43</td> <td>41</td> </tr> </tbody> </table> <p>Carry out an Analysis of variances</p>		Salesmen				Season	1	2	3	4	Summer	45	40	28	37	Winter	43	41	45	38	Monsoon	39	39	43	41	BTL -3	Applying
	Salesmen																											
Season	1	2	3	4																								
Summer	45	40	28	37																								
Winter	43	41	45	38																								
Monsoon	39	39	43	41																								
14.	<p>The following data resulted from an experiment to compare three burners A, B, C. A Latin square design was used as the tests were made on 3 engines and were spread over 3 days.</p> <table border="1" data-bbox="507 584 932 696"> <tbody> <tr> <td>A 16</td> <td>B 17</td> <td>C 20</td> </tr> <tr> <td>B 16</td> <td>C 21</td> <td>A 15</td> </tr> <tr> <td>C 15</td> <td>A 12</td> <td>B 13</td> </tr> </tbody> </table> <p>Test the hypothesis and infer that there is no difference between the burners.</p>	A 16	B 17	C 20	B 16	C 21	A 15	C 15	A 12	B 13	BTL -4	Creating																
A 16	B 17	C 20																										
B 16	C 21	A 15																										
C 15	A 12	B 13																										
15.	<p>A farmer wishes to test the effects of four different fertilizers A,B,C, Don the yield of Wheat. In order to eliminate sources of error due to variability in soil fertility, he uses the fertilizers, in a Latin square arrangement a syndicated in the following table, where the numbers indicate yields per unit area.</p> <table border="1" data-bbox="379 882 1059 1032"> <tbody> <tr> <td>A18</td> <td>C21</td> <td>D25</td> <td>B11</td> </tr> <tr> <td>D22</td> <td>B12</td> <td>A15</td> <td>C19</td> </tr> <tr> <td>B15</td> <td>A20</td> <td>C23</td> <td>D24</td> </tr> <tr> <td>C22</td> <td>D21</td> <td>B10</td> <td>A17</td> </tr> </tbody> </table> <p>Design an analysis of variance to determine if there is a significant difference between the fertilizers at $\alpha=0.05$ and $\alpha=0.01$ levels of significance.</p>	A18	C21	D25	B11	D22	B12	A15	C19	B15	A20	C23	D24	C22	D21	B10	A17	BTL -3	Applying									
A18	C21	D25	B11																									
D22	B12	A15	C19																									
B15	A20	C23	D24																									
C22	D21	B10	A17																									
16.	<p>Set up the analysis of variance for the following results of a Latin Square Design(use $\alpha = 0.01$) level of significance</p> <table border="1" data-bbox="400 1178 1035 1346"> <tbody> <tr> <td>A12</td> <td>C19</td> <td>B10</td> <td>D8</td> </tr> <tr> <td>C18</td> <td>B12</td> <td>D6</td> <td>A7</td> </tr> <tr> <td>B22</td> <td>D10</td> <td>A5</td> <td>C21</td> </tr> <tr> <td>D12</td> <td>A7</td> <td>C27</td> <td>B17</td> </tr> </tbody> </table>	A12	C19	B10	D8	C18	B12	D6	A7	B22	D10	A5	C21	D12	A7	C27	B17	BTL -4	Creating									
A12	C19	B10	D8																									
C18	B12	D6	A7																									
B22	D10	A5	C21																									
D12	A7	C27	B17																									
17.	<p>In a 5x5 Latin square experiment, the data collected is given in the matrix below Yield per plot is given in quintals for the five different cultivation treatments A, B, C,D and E. Perform the analysis of variance.</p> <table data-bbox="448 1420 1233 1637"> <tr> <td>A48</td> <td>E66</td> <td>D56</td> <td>C52</td> <td>B61</td> </tr> <tr> <td>D64</td> <td>B62</td> <td>A50</td> <td>E64</td> <td>C63</td> </tr> <tr> <td>B69</td> <td>A53</td> <td>C60</td> <td>D61</td> <td>E67</td> </tr> <tr> <td>C57</td> <td>D58</td> <td>E67</td> <td>B65</td> <td>A55</td> </tr> <tr> <td>E67</td> <td>C57</td> <td>B66</td> <td>A60</td> <td>D57</td> </tr> </table>	A48	E66	D56	C52	B61	D64	B62	A50	E64	C63	B69	A53	C60	D61	E67	C57	D58	E67	B65	A55	E67	C57	B66	A60	D57	BTL -3	Applying
A48	E66	D56	C52	B61																								
D64	B62	A50	E64	C63																								
B69	A53	C60	D61	E67																								
C57	D58	E67	B65	A55																								
E67	C57	B66	A60	D57																								
18.	<p>A variable trial was conducted on wheat with 4 varieties in a Latin square design. The plan of the experiment and the per plot yield are given below.</p> <table data-bbox="432 1715 762 1854"> <tr> <td>C25</td> <td>B23</td> <td>A20</td> <td>D20</td> </tr> <tr> <td>A19</td> <td>D19</td> <td>C21</td> <td>B18</td> </tr> <tr> <td>B19</td> <td>A14</td> <td>D17</td> <td>C20</td> </tr> <tr> <td>D17</td> <td>C20</td> <td>B21</td> <td>A15</td> </tr> </table>	C25	B23	A20	D20	A19	D19	C21	B18	B19	A14	D17	C20	D17	C20	B21	A15	BTL -4	Creating									
C25	B23	A20	D20																									
A19	D19	C21	B18																									
B19	A14	D17	C20																									
D17	C20	B21	A15																									

UNIT-V: TIME SERIES ANALYSIS

12

Time series as a discrete stochastic process. Stationarity- Main characteristics of stochastic process (mean, auto co variation and auto correlation function)-Autoregressive models AR (p) -Yull-Worker equation Auto regressive moving average models ARMA.

PART – A

Q.No.	Question	BTL Level	Competence																		
1.	Define Discrete Random Process with example.	BTL -1	Remembering																		
2.	Define wide sense stationary process.	BTL -1	Remembering																		
3.	What are the four types of a stochastic process?	BTL -1	Remembering																		
4.	Derive the auto correlation for a Poisson process with rate λ .	BTL -1	Remembering																		
5.	A random process $X(t) = A \sin t + B \cos t$ where A and B are independent random variables with zero means and equal standard deviations. Find the mean of the process.	BTL -1	Remembering																		
6.	Find the mean of a stationary random process whose auto correlation function is given by $R_{(Z)} = \frac{25Z^2 + 36}{6.25Z^2 + 4}$	BTL -1	Remembering																		
7.	Define Time Series Analysis	BTL -2	Understanding																		
8.	Why should we learn Time Series?	BTL -2	Understanding																		
9.	How many Components of Time Series?	BTL -2	Understanding																		
10.	Explain Cyclic Variations	BTL -2	Understanding																		
11.	How can be Seasonality assessed using graphical procedures?	BTL -1	Applying																		
12.	Write the Formula for Multiplicative Model in Time Series?	BTL -1	Applying																		
13.	List the methods for Measurements of Trends?	BTL -1	Applying																		
14.	Fit a trend line by the method of freehand method for the given data. <table border="1" style="margin-left: 20px;"> <tr> <td>Year</td> <td>2000</td> <td>2001</td> <td>2002</td> <td>2003</td> <td>2004</td> <td>2005</td> <td>2006</td> <td>2007</td> </tr> <tr> <td>Sales</td> <td>30</td> <td>46</td> <td>25</td> <td>59</td> <td>40</td> <td>60</td> <td>38</td> <td>65</td> </tr> </table>	Year	2000	2001	2002	2003	2004	2005	2006	2007	Sales	30	46	25	59	40	60	38	65	BTL -2	Analyzing
Year	2000	2001	2002	2003	2004	2005	2006	2007													
Sales	30	46	25	59	40	60	38	65													
15.	What are the Process Model for a Time Series?	BTL -1	Analyzing																		
16.	Define White Noise Process?	BTL -2	Analyzing																		
17.	What is First order Markov Process?	BTL -1	Analyzing																		
18.	Define AR process	BTL -2	Analyzing																		
19.	Explain Auto regressive process of order 2	BTL -2	Creating																		
20.	Which treatment(s) for seasonality ?	BTL -1	Analyzing																		
21.	Define Discrete Random sequence with example.	BTL -1	Applying																		
22.	Define Discrete Random Process with example.	BTL -1	Applying																		
23.	Compute the mean value of the random process whose auto correlation function is given by $R_{XX}(\tau) = 25 + \frac{4}{1+6\tau^2}$.	BTL -1	Applying																		
24.	Find the mean of a stationary random process whose auto correlation function is given by $R_{XX}(\tau) = 18 + \frac{2}{6+\tau^2}$.	BTL -1	Analyzing																		
25.	Define Box –Jenkins model	BTL -2	Analyzing																		

PART – B

1.	The process $\{X(t)\}$ whose probability distribution under certain conditions is given by $P\{X(t) = n\} = \begin{cases} \frac{(at)^{n-1}}{(1+at)^{n+1}}, & n = 1, 2 \\ \frac{at}{(1+at)}, & n = 0 \end{cases}$ Show that it is not stationary.	BTL -3	Applying
2.	The probability of a dry day following a rainy day is $1/3$ and the at the probability of a rainy day following a dry day is $1/2$. Given that May 1 st is a dry day. Find the probability that May 3 rd is a dry day also May 5 th is a dry day.	BTL -4	Creating

3.	Describe Co-variance stationary of Auto Regressive Process of order 2 (Yule Process)	BTL -3	Applying																												
4.	Calculate three-yearly moving averages of number of students studying in a higher secondary school in a particular village from the following data. <table border="1"> <tr> <td>Year</td> <td>1995</td> <td>1996</td> <td>1997</td> <td>1998</td> <td>1999</td> </tr> <tr> <td>Sales</td> <td>332</td> <td>317</td> <td>357</td> <td>392</td> <td>402</td> </tr> <tr> <td>Year</td> <td>2000</td> <td>2001</td> <td>2002</td> <td>2003</td> <td>2004</td> </tr> <tr> <td>Sales</td> <td>405</td> <td>410</td> <td>427</td> <td>435</td> <td>438</td> </tr> </table>	Year	1995	1996	1997	1998	1999	Sales	332	317	357	392	402	Year	2000	2001	2002	2003	2004	Sales	405	410	427	435	438	BTL -4	Creating				
Year	1995	1996	1997	1998	1999																										
Sales	332	317	357	392	402																										
Year	2000	2001	2002	2003	2004																										
Sales	405	410	427	435	438																										
5.	If the customers arrive in accordance with the Poisson process, with rate of 2 per minute, Find the probability that the interval between 2 consecutive arrivals is (i) more than 1 minute, (ii) between 1 and 2 minutes, (iii) less than 4 minutes.	BTL -3	Applying																												
6.	The sales of a commodity in tones varied from January 2010 to December 2010 as follows: <table border="1"> <tr> <td>Month</td> <td>Jan</td> <td>Feb</td> <td>Mar</td> <td>Apr</td> <td>May</td> <td>June</td> </tr> <tr> <td>Sales</td> <td>280</td> <td>240</td> <td>270</td> <td>300</td> <td>280</td> <td>290</td> </tr> <tr> <td>Month</td> <td>July</td> <td>Aug</td> <td>Sep</td> <td>Oct</td> <td>Nov</td> <td>Dec</td> </tr> <tr> <td>Sales</td> <td>210</td> <td>200</td> <td>230</td> <td>200</td> <td>230</td> <td>210</td> </tr> </table> Fit a Trend the line by the method of Semi-Average	Month	Jan	Feb	Mar	Apr	May	June	Sales	280	240	270	300	280	290	Month	July	Aug	Sep	Oct	Nov	Dec	Sales	210	200	230	200	230	210	BTL -4	Creating
Month	Jan	Feb	Mar	Apr	May	June																									
Sales	280	240	270	300	280	290																									
Month	July	Aug	Sep	Oct	Nov	Dec																									
Sales	210	200	230	200	230	210																									
7.	Prove that the difference of two independent Poisson process is not a Poisson process.	BTL -3	Applying																												
8.	The following figures relates to the profits of a commercial concern for 8 years <table border="1"> <tr> <td>Year</td> <td>1986</td> <td>1987</td> <td>1988</td> <td>1989</td> <td>1990</td> <td>1991</td> <td>1992</td> <td>1993</td> </tr> <tr> <td>Profit</td> <td>15420</td> <td>15470</td> <td>15520</td> <td>21020</td> <td>26500</td> <td>31950</td> <td>35600</td> <td>34900</td> </tr> </table> Find the trend of profits by the method of three yearly moving Average	Year	1986	1987	1988	1989	1990	1991	1992	1993	Profit	15420	15470	15520	21020	26500	31950	35600	34900	BTL -4	Creating										
Year	1986	1987	1988	1989	1990	1991	1992	1993																							
Profit	15420	15470	15520	21020	26500	31950	35600	34900																							
9.	A salesman's territory consists of three regions A, B, C. He never sells in the same region on successive days. If he sells in region A, then the next day he sells in B. However, if he sells either B or C, then the next day he is twice as likely to sell in A as in the other region. Explain How often does he sell in each of the regions in the steady state?	BTL -3	Applying																												
10.	Check whether the Poisson process $X(t)$ given by the probability law $P\{X(t) = n\} = \frac{e^{-\lambda t}(\lambda t)^n}{n!}, n = 0,1,2, \dots$ is stationary or not.	BTL -4	Creating																												
11.	Write the short notes of models of time series	BTL -3	Applying																												
12.	Explain ARMA process with suitable example.	BTL -4	Creating																												
13.	Fit a trend line by the method of semi- averages for the given data. <table border="1"> <tr> <td>Year</td> <td>1990</td> <td>1991</td> <td>1992</td> <td>1993</td> <td>1994</td> <td>1995</td> <td>1996</td> <td>1997</td> </tr> <tr> <td>Sales</td> <td>15</td> <td>11</td> <td>20</td> <td>10</td> <td>15</td> <td>25</td> <td>35</td> <td>30</td> </tr> </table>	Year	1990	1991	1992	1993	1994	1995	1996	1997	Sales	15	11	20	10	15	25	35	30	BTL -3	Applying										
Year	1990	1991	1992	1993	1994	1995	1996	1997																							
Sales	15	11	20	10	15	25	35	30																							
14.	Find the trend of annual sales of a trading organization by Moving Average Method: <table border="1"> <tr> <td>Year</td> <td>Annual Sales (Rs. In '000)</td> <td>Year</td> <td>Annual Sales (Rs. In '000)</td> </tr> <tr> <td>1964</td> <td>80</td> <td>1974</td> <td>84</td> </tr> <tr> <td>1965</td> <td>84</td> <td>1975</td> <td>96</td> </tr> <tr> <td>1966</td> <td>80</td> <td>1976</td> <td>92</td> </tr> <tr> <td>1967</td> <td>88</td> <td>1977</td> <td>104</td> </tr> </table>	Year	Annual Sales (Rs. In '000)	Year	Annual Sales (Rs. In '000)	1964	80	1974	84	1965	84	1975	96	1966	80	1976	92	1967	88	1977	104	BTL -4	Creating								
Year	Annual Sales (Rs. In '000)	Year	Annual Sales (Rs. In '000)																												
1964	80	1974	84																												
1965	84	1975	96																												
1966	80	1976	92																												
1967	88	1977	104																												

		1968	98	1978	116				
		1969	92	1979	112				
		1970	84	1980	102				
		1971	88	1981	114				
		1972	80	1982	108				
		1973	100	1983	126				
	(Use the most appropriate period of moving average)								
15.	Show that the random process $X(t) = A\cos\omega t + B\sin\omega t$ is wide sense stationary process if A and B are random variables such that $E(A) = E(B) = 0, E(A^2) = E(B^2)$ and $E(AB) = 0$						BTL -3	Applying	
16.	The sales of a commodity in tones varied from January 2020 to December 2020 as follows:						BTL -4	Creating	
	Month	Jan	Feb	Mar	Apr	May			June
	Sales	210	200	230	200	230			210
	Month	July	Aug	Sep	Oct	Nov			Dec
	Sales	280	240	270	300	280			290
	Fit a Trend the line by the method of Semi-Average								
17.	Three boys A, B and C are throwing a ball to each other. A always throws the ball to B and B always throws the ball to C but C is just as likely to throw the ball to B as to A. Show that the process is Markovian. Find the transition probability matrix and classify the states						BTL -3	Applying	
18.	Write the short notes of Yull-Worker equation Auto regressive moving average models						BTL -4	Creating	